## Geometric Vectors (Solution)

7. In the figure, the tip of $\mathbf{c}$ and the tail of $\mathbf{d}$ are both the midpoint of $Q R$. Express $\mathbf{c}$ and $\mathbf{d}$ in terms of $\mathbf{a}$ and $\mathbf{b}$

(1) Redraw and finish the parallelgram:


Q12.2-7 from Calculus: Early Transcendentals Te by Stewart
Why: Want to express c and d in terms of a and b .
Steps:

1. Complete the parallelogram to find $a+b$ and $a-b, b-a$
2. Express $c$ and $d$ in terms of $a$ and $b$
(2)

$$
\begin{array}{ll}
2 \vec{c}=\vec{a}+\vec{b} & 2 \vec{d}=\vec{b}-\vec{a} \\
\vec{c}=\frac{1}{2} \vec{a}+\frac{1}{2} \vec{b} & \vec{d}=\frac{1}{2} \vec{b}-\frac{1}{2} \vec{a}
\end{array}
$$

You can also use
$\vec{d}=-\vec{c}+\vec{b}$
$\vec{d}=-\frac{1}{2} \vec{a}-\frac{1}{2} \vec{b}+\vec{b}$
$\vec{d}=\frac{1}{2} \vec{b}-\frac{1}{2} \vec{a}$


